CH 3: Differentiation Rules

3.1 Derivatives of Polynomials and Exponential Functions

- 1. $\frac{d}{dx}f(x)$ is another notation for f'(x) that points out the variable you must take the derivative with respect to, namely x captured by the dx in the denominator.
- 2. constants: $\frac{d}{dx}(\text{constant}) = 0$
- 3. the **power rule**: $\frac{d}{dx}(x^n) = nx^{n-1}$, for all real numbers *n*, particularly $\frac{d}{dx}(x) = 1$
- 4. the sum rule: $\frac{d}{dx}f(x) + \frac{d}{dx}g(x) = \frac{d}{dx}(f(x) + g(x))$. Example: $\frac{d}{dx}(x^7 + x) = 7x^6 + 1$
- 5. the **difference rule**: $\frac{d}{dx}f(x) \frac{d}{dx}g(x) = \frac{d}{dx}(f(x) g(x)).$ Example: $\frac{d}{dx}(\sqrt{x} 3) = \frac{d}{dx}\sqrt{x} \frac{d}{dx}3 = \frac{1}{2}x^{-\frac{1}{2}} 0 = \frac{1}{2\sqrt{x}}$
- 6. the constant multiple rule: $\frac{d}{dx}(c \cdot f(x)) = c \frac{d}{dx}f(x).$ Example: $\frac{d}{dx}(3x^{-7}) = 3 \cdot \frac{d}{dx}(x^{-7}) = 3 \cdot (-7)x^{-6} = -21x^{-6}$
- 7. $f'(0) = \lim_{h \to 0} \frac{e^h e^0}{h} = 1$, meaning that the function e^x has a tangent line with a slope of 1 at x = 0
- 8. the derivative of the natural exponential function: $\frac{d}{dx}(e^x) = e^x$,
- 9. the derivative of the natural log function: $\frac{d}{dx}(\ln |x|) = \frac{1}{x}$,
- 10. recall: the **secant line** to a curve is the line that goes through 2 points on the graph (if the graph represents distance, then its slope is the average speed between the two points)
- 11. recall: the **tangent line** to a curve is the line that touches the graph exactly once at that point (if the graph represents distance, then its slope is the instantaneous speed at that point)
- 12. we define the **normal line** to a curve is the line that is perpendicular to the tangent line (if we have a 3-dimensional surface, then we have a tangent plane that touches the surface at exactly one point, and the normal line is perpendicular to each line in this tangent plane and it helps find the equation of the plane you'll see this in MA1115)